First observation of $B^0 \to D^{*0} \pi^+ \pi^- \pi^- \pi^-$ decays

We report on the observation of $B^0 \to D^{*0} \pi^+ \pi^- \pi^- \pi^-$ decays. The branching ratio is $(0.30 \pm 0.07 \pm 0.06)\%$. Interest in this particular mode was sparked by Ligeti, Luke and Wise who propose it as a way to check the validity of factorization tests in $B^0 \to D^{*+} \pi^- \pi^- \pi^0$ decays.

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Factorization is the assumption that in two-body hadronic \( B \) decays the decay amplitude can be expressed as a product of two currents, just as in semileptonic decays where one current is hadronic and the other leptonic. Use of factorization has been crucial in creating models for understanding the underlying weak decay dynamics [1].

In previous work we found a large branching fraction of \((1.72 \pm 0.14 \pm 0.24)\%\) for the decay \( \bar{B}^0 \rightarrow D^{\ast} \pi^+ \pi^- \pi^- \pi^0 \) \([2]\). This reaction can proceed via several possible tree level processes. The simplest diagram, shown in Fig. 1(a), has the four pions emitted from the virtual \( W^- \). Assuming that this is indeed the dominant process, Ligeti, Luke and Wise (LLW) \([3]\) have compared the \(4\pi^-\) invariant mass spectrum with \( \tau^- \rightarrow \pi^+ \pi^- \pi^- \pi^0 \nu \) data \([4]\). Using a model based on factorization they show that the data agree up to a \(4\pi^-\) mass-squared of 2.9 GeV\(^2\), within a precision of about 15%.

However, the agreement may be fortuitous, rather than a success of factorization, if other diagrams are present. For example another possible diagram is shown in Fig. 1(b), where the \( D^{\ast} \) and the \( \pi^0 \) are produced at the lower vertex and the virtual \( W^- \) manifests as \( \pi^+ \pi^- \pi^- \). This process was searched for in the original publication. Definite evidence was lacking but a stringent upper limit could not be set.

Here we search for the process \( \bar{B}^0 \rightarrow D^{\ast} \pi^+ \pi^- \pi^- \pi^- \) as suggested by LLW. This can be produced by the diagram in Fig. 1(b), where the \( D^{\ast} \) combines with one of the \( \pi^+ \)s to form a low-mass system. It could also be produced by the color-suppressed process shown in Fig. 1(c). In this paper we indeed show that the process \( \bar{B}^0 \rightarrow D^{\ast} \pi^+ \pi^- \pi^- \pi^- \) has a significant branching ratio and try to ascertain the dominant production mechanism. The data sample consists of 9.0 fb\(^{-1}\) of integrated luminosity taken with the CLEO II and II.L detectors \([5]\) using the Cornell Electron Storage Ring (CESR) on the peak of the \(Y(4S)\) resonance and 4.4 fb\(^{-1}\) in the continuum at 60 MeV less center-of-mass energy. The sample contains 19.4 million \( B \) mesons.

Hadronic events are selected by requiring a minimum of five charged tracks, total visible energy greater than 15% of the center-of-mass energy, and a charged track vertex consistent with the nominal interaction point. To reject non-\(B\bar{B}\) continuum we require that the Fox-Wolfram moment \( R_2 \) be less than 0.3 [6]. Track candidates are required to pass through a common spatial point defined by the luminous region. Tracks with momenta below 900 MeV/c are required to have an ionization loss in the drift chamber within 3 standard deviations of that expected for their mass hypothesis (\( \pi/K \)). Photon candidates are required to be in the “good barrel region,” within 45° of the plane perpendicular to the beam line that passes through the interaction point, and have an energy distribution in the CsI calorimeter consistent with that of an electromagnetic shower. To select \( \pi^0 \)s, we require that the diphoton invariant mass be between \(-3.0 \pm 2.5\sigma\) of the \( \pi^0\) mass, where the resolution \( \sigma \) varies with momentum and has an average value of approximately 5.5 MeV. The \( \pi^0 \) candidates are then kinematically fit by constraining their invariant mass to be equal to the nominal \( \pi^0 \) mass.

We select \( D^{\ast} \) candidates in the \( K^- \pi^+ \) decay mode. We require that the invariant mass of the \( D^{\ast} \) candidates lie within \(\pm 2.5\sigma\) of the known \( D^0 \) mass. The \( D^{\ast} \) mass resolution varies with \( D^0 \) momentum, \( p \), as \( p \times 0.93 \times 10^{-3} + 6.0 \) (units of MeV). We use the analogous requirement on the \( D^{\ast} - D^0 \) mass difference. In this case the mass difference resolution is 0.90 MeV.

We start by looking for the \( D^{\ast +} (4\pi^0) \) final state.\(^{1}\) The \( D^{\ast +} \) candidates are pooled with all combinations of \( \pi^+ \pi^- \pi^- \) mesons. Next, we calculate the difference between the beam energy, \( E_{\text{beam}} \), and the measured energy of the five particles, \( \Delta E \). The “beam constrained” invariant mass of the \( B \) candidates, \( M_B \), is computed from the formula \( M_B^2 = E_{\text{beam}}^2 - (\sum_{i} p_i)^2 \). To further reduce backgrounds we define

\[
\chi_B^2 = \left( \frac{\Delta M_{D^{\ast +}}}{\sigma (\Delta M_{D^{\ast +}})} \right)^2 + \left( \frac{M(K \pi^-) - M_{D^{\ast +}}}{\sigma (M(K \pi^-) - M_{D^{\ast +}})} \right)^2 + \left( \frac{M(\gamma \gamma) - M_{\pi^0}}{\sigma (M(\gamma \gamma) - M_{\pi^0})} \right)^2,
\]

where \( \Delta M_{D^{\ast +}} \) is the computed \( D^{\ast +} - D^0 \) mass difference minus the nominal value and the \( \sigma \)’s are the measurement errors. We select candidate events requiring that \( \chi_B^2 < 5 \).

\(^{1}\)In this paper \( (4\pi^0) \) will always denote the specific combination \( \pi^+ \pi^- \pi^- \pi^- \).

FIG. 1. Diagrams for \( \bar{B} \rightarrow D^{\ast} \pi^+ \pi^- \pi^- \pi^- \) decays. (a) Charged current tree level diagram for \( D^{\ast +} (4\pi^-) \). (b) Charged current tree level diagram for \( (D^{\ast +} \pi^0) \pi^- \pi^- \pi^- \) or \( (D^{\ast 0} \pi^+) \pi^+ \pi^- \) \pi^- \pi^- \). The \( D^{\ast} \) system can form a \( D^{\ast \ast} \) resonance. (c) Color suppressed diagram for \( D^{\ast 0} (4\pi^0) \).
We show the candidate $B$ mass distribution, $M_B$, for $\Delta E$ in the side-bands from $-6.0$ to $-4.0\sigma$ and $4.0$ to $6.0\sigma$ on Fig. 2(a). The $\Delta E$ resolution is $14$ MeV ($\sigma$). The sidebands give a good representation of the background in the signal region. We fit this distribution with a shape given as 
\[
\text{back}(r) = p_1 r \sqrt{1 - r^2} e^{-r^2}.
\]
where $r = M_B/5.2895$, and the $p_i$ are parameters given by the fit.

We next view the $M_B$ distribution for events having $\Delta E$ within $2\sigma$ of zero in Fig. 2(b). This distribution is fit with a Gaussian signal function of width $2.7$ MeV and the background function found above whose normalization is allowed to vary. The Gaussian signal width is found from Monte Carlo simulation. The largest and dominant component results from the energy spread of the beam. We find a total of $64 \pm 16$ events, thus establishing a signal.

The error due to the background shape is evaluated in three ways. First of all, we change the background shape by varying the fitted parameters by $1\sigma$. This results in a change of $\pm 9.3\%$. Secondly, we allow the shape, $p_2$, to vary (the normalization, $p_1$, was already allowed to vary). This results in $11\%$ decrease in the number of events. Finally, we choose a different background function, 
\[
\text{back'}(r) = p_1 r \sqrt{1 - r^2} (1 + p_2 r + p_3 r^2 + p_4 r^3),
\]
and repeat the fitting procedure. This results in a $9.3\%$ increase in the number of events. We assign $\pm 7$ events system error due to this source.

We have investigated two mode-specific backgrounds that could, in principle, induce fake signals. These include the final states $D^{*+}\pi^-\pi^+\pi^-\pi^0$, where we miss the slow $\pi^-$ from the $D^{*+}$ decay and the $\pi^0$ and $D^0$ happen to satisfy the $D^{*0}$ requirement, and $D^0\pi^+\pi^-\pi^+\pi^-$, where the $D^0$ and the $\pi^0$ happen to satisfy the $D^{*0}$ requirement. We find that the efficiencies for each of these modes to contribute are small. The first final state was measured as having a branching ratio of $1.72\%$ [2]. It would contribute $0.4 \pm 0.5$ events. The second final state has never been measured. It would contribute $1.6 \pm 0.5$ events per $1\%$ branching ratio. Taking into account all sources of systematic error we observe $64 \pm 16 \pm 7$ signal events.

In order to find the branching ratio we use the Monte Carlo–determined efficiency, shown in Fig. 3 as a function of $(4\pi)^0$ mass. Since the efficiency varies with mass we need to determine the $(4\pi)^0$ mass spectrum in order to determine the branching ratio. To rid ourselves of the problem of the background shape, we fit the $B$ candidate mass spectrum in $100$ MeV bins of $(4\pi)^0$ mass. The resulting $(4\pi)^0$ mass spectrum is shown in Fig. 4. We find

\[
\mathcal{B}(\bar{B}^0 \to D^{*0}\pi^+\pi^-\pi^+\pi^-) = (0.30 \pm 0.07 \pm 0.06)\%.
\]

The systematic error arises mainly from our lack of knowledge about the tracking and $\pi^0$ efficiencies. We assign errors

![FIG. 2. The $B$ candidate mass spectra for the final state $D^{*0}\pi^+\pi^-\pi^+\pi^-$. (a) $\Delta E$ sidebands; (b) for $\Delta E$ consistent with zero.](image1)

![FIG. 3. The efficiency for the final state $D^{*0}\pi^+\pi^-\pi^+\pi^-$.](image2)

![FIG. 4. The invariant mass spectrum of $\pi^+\pi^+\pi^-\pi^-$ for the final state $D^{*0}\pi^+\pi^-\pi^+\pi^-$.](image3)
of ±2.2% on the efficiency of each charged track, and ±5.4% for the π0. The total tracking error is found by adding the error in the charged particle track finding efficiency linearly for the 6 “fast” charged tracks and then in quadrature with the slow pion from the D*0 decay. The error on the background shape has been discussed above. We take a conservative estimate of the systematic error due to this source of ±11%. We use the current Particle Data Group values for the relevant D*0 and D0 branching ratios of (61.9±2.9)% (D*0→π0D0) and (3.83±0.09)% (D0→K−π+) [7]. The relative errors, 4.7% for the D*0 branching ratio and 2.3% for the D0 are added in quadrature to the background shape error, the π0 detection efficiency uncertainty and the tracking error. The total positive systematic error is 19%. We also allow for cross-feed backgrounds amounting to 4 events giving a total negative systematic error of 20%.

In Fig. 5(a) we show the D*0π+ invariant mass spectrum, obtained by fitting the number of B0 events as a function of D*0π+ mass. (There are two combinations per event.) We also show for comparison the D*0π− mass spectrum, where no structure is expected. We see evidence for an excess of events in the region of the D**+(2420) and D**+(2460). There are four D** mesons. Two have relatively narrow widths and decay into D* π, whereas two are wide, with only one decaying into D* π [8]. It is difficult to quantitatively evaluate the fraction of total D**+ production in our data. We find that ~70% of the signal has one mass combination between 2.3 and 2.6 GeV.

In Fig. 6 we show the π+π−π− mass spectrum when the D*0π+ mass is required to be between 2.3 and 2.6 GeV. Here we fit the B yield as a function of π+π−π− mass. There is no clear feature present.

Let us now see how the presence of this final state affects the LLW prediction. In Fig. 7 we show the CLEO data [2] for (dΓ/dM2)(B0→D*+ π+ π−π0) plotted as a function of the four-pion invariant mass squared, normalized to the semileptonic rate [7], and compared with the LLW prediction [3]. We also plot (dΓ/dM2)(B0→D*0π+ π−π−π0), again normalized to the semileptonic rate. In principle a non-zero excess of events in the region of the D**+(2420) and D**+(2460). There are four D** mesons. Two have relatively narrow widths and decay into D* π, whereas two are wide, with only one decaying into D* π [8]. It is difficult to quantitatively evaluate the fraction of total D**+ production in our data. We find that ~70% of the signal has one mass combination between 2.3 and 2.6 GeV.
rate in the $D^{*0}(4\pi)^0$ final state is indicative of an additional contribution to the $D^{*+}(4\pi)^-$ final state, beyond what is expected in factorization, and needs to be subtracted to make an accurate prediction. In fact, the $D^{*0}(4\pi)^0$ rate is consistent with zero in the mass squared region covered by the LLW prediction.

In conclusion we have made the first measurement of $B(\bar{B}^0 \rightarrow D^{*0}\pi^+\pi^+\pi^-\pi^-) = (0.30 \pm 0.07 \pm 0.06)\%$. The reaction has a large component of $D^{*+\pi^0} \rightarrow D^{*0}\pi^+$. We determine the relative rate

$$R_{0-} = \frac{\Gamma(\bar{B}^0 \rightarrow D^{*0}\pi^+\pi^+\pi^-\pi^-)}{\Gamma(\bar{B}^0 \rightarrow D^{*+\pi^0}\pi^-\pi^-)} = 0.17 \pm 0.04 \pm 0.02.$$ (3)

We have no evidence in the $D^{*0}$ final state for $4\pi^0$ masses below $2.9\text{ GeV}^2$ and set an upper limit on $R_{0-} < 0.13$ at 90% confidence level in this restricted mass region.

LLW have used the $\bar{B}^0 \rightarrow D^{*+}\pi^+\pi^-\pi^0$ reaction to test the $4\pi$ mass dependence of factorization. They point out that a perturbative origin for factorization should cause a weakening of the prediction with increasing $4\pi$ mass. However if the basis for factorization is the large $N_c$ limit, where $N_c$ refers to the number of colors, no such weakening should occur. LLW also suggest that the presence of $D^{**}$ production might cause their factorization test to be inaccurate. We have found such a presence in the analogous reaction $\bar{B}^0 \rightarrow D^{*0}\pi^+\pi^+\pi^-\pi^-$. However, the $4\pi$ mass region that is populated is higher than that used by LLW, so no effect on their prediction can be inferred.

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